Structured Tree Alignment for Evaluation of (Speech) Constituency Parsing

Freda Shi  Kevin Gimpel  Karen Livescu
Toyota Technological Institute at Chicago
6045 S. Kenwood Ave, Chicago, IL, USA, 60637
{freda,kgimpel,klivescu}@ttic.edu

Abstract

We present the structured average intersection-over-union ratio (STRUCT-IU), a similarity metric between constituency parse trees motivated by the problem of evaluating speech parsers. STRUCT-IU enables comparison between a constituency parse tree (over automatically recognized spoken word boundaries) with the ground-truth parse (over written words). To compute the metric, we project the ground-truth parse tree to the speech domain by forced alignment, align the projected ground-truth constituents with the predicted ones under certain structured constraints, and calculate the average IOU score across all aligned constituent pairs. STRUCT-IU takes word boundaries into account and overcomes the challenge that the predicted words and ground truth may not have perfect one-to-one correspondence. Extending to the evaluation of text constituency parsing, we demonstrate that STRUCT-IU shows higher tolerance to syntactically plausible parses than PARSVAL (Black et al., 1991).

1 Introduction

Automatic constituency parsing of written text (Marcus et al., 1993, inter alia) and speech transcriptions (Godfrey and Holliman, 1993, inter alia), as representative tasks of automatic syntactic analysis, have been widely explored in the past few decades. Appropriate evaluation metrics have facilitated the comparison and benchmarking of different approaches: the PARSVAL $F_1$ score (Black et al., 1991; Sekine and Collins, 1997) has served as a reliable measure of text parsing across various scenarios; for speech transcription parsing, SPARSIVAL (Roark et al., 2006), which extends PARSIVAL and accounts for speech recognition errors by allowing word-level editing with a cost, has been commonly used.

Recent work (Lai et al., 2023; Tseng et al., 2023) has proposed the related task of textless speech constituency parsing. In contrast to earlier work that parses manually labeled (Charniak and Johnson, 2001, inter alia) or automatic (Kahn and Ostendorf, 2012, inter alia) speech transcriptions, these models construct constituency parse trees over automatically recognized spoken word boundaries, where each word is represented with a time range of the spoken utterance, without using any form of text. To evaluate these textless models, we need a metric that compares the predicted tree (over spoken word boundaries) with the manually labeled ground-truth tree (over written words) and faithfully reflects the parsing quality. Since the automatically recognized word boundaries may be imperfect, the metric should also reflect the changes...
in parsing quality due to word boundary errors. To the best of our knowledge, none of the existing metrics meets these requirements, as they are all designed to compare parse trees over discrete word sequences, instead of continuous time ranges.

Motivated by the need for textless speech parsing evaluation, in this paper, we introduce the structured average intersection-over-union ratio ($\text{STRUCT-IOU};$ Figure 1), a metric that compares two parse trees over time ranges. We relax the definition of segment trees (Bentley, 1977) to represent speech constituency parse trees, where each node is associated with an interval that represents the time range of the corresponding spoken word or constituent. To obtain the “ground-truth” speech parse trees, we use the forced alignment algorithm (McAuliffe et al., 2017), a supervised and highly accurate method that aligns written words to time ranges of the corresponding spoken utterance, to project the ground-truth text parses onto the time domain. $\text{STRUCT-IOU}$ is calculated by aligning the same-label nodes in the predicted and ground-truth parse trees, following structured constraints that preserve parent-child relations. The calculation of $\text{STRUCT-IOU}$ can be formulated as an optimization problem (§4.1) with a polynomial-time solution (§4.2) in terms of the number of tree nodes.

Although $\text{STRUCT-IOU}$ is designed to evaluate speech parsing, it is also applicable to text parsing evaluation. We analyze $\text{STRUCT-IOU}$ for both purposes: in speech parsing evaluation, $\text{STRUCT-IOU}$ robustly takes into account both the structure information and word boundaries; in text parsing evaluation, while maintaining a high correlation with the $\text{PARSEVAL F}_1$ score, $\text{STRUCT-IOU}$ shows a higher tolerance to potential syntactic ambiguity.

2 Related Work

Text constituency parsing and evaluation. In the past decades, there has been much effort in building and improving constituency parsing models (Collins and Koo, 2005; Charniak and Johnson, 2005; McClosky et al., 2006; Durrett and Klein, 2015; Cross and Huang, 2016; Dyer et al., 2016; Choe and Charniak, 2016; Stern et al., 2017; Kitaev and Klein, 2018, inter alia). $\text{PARSEVAL}$ (Black et al., 1991) has been the standard evaluation metric for constituency parsing in most scenarios, which takes the ground truth and predicted trees and calculates the harmonic mean of precision and recall of labeled spans. For morphologically rich languages, $\text{TED\textsc{EVAL}}$ (Tsarfaty et al., 2012) extends $\text{PARSEVAL}$ to accept multiple morphological analyses over sequences of words. All of these metrics are designed to evaluate parses over discrete word sequences, and cannot be easily extended to evaluate speech parses over continuous time ranges. Although our metric, $\text{STRUCT-IOU}$, is designed to evaluate speech constituency parsing, it can be easily extended for text parsing evaluation, reflecting a different aspect from existing metrics (§5.2).

Speech constituency parsing and its evaluation. Work on conversational speech parsing has focused on addressing the unique challenges posed by speech, including speech recognition errors (Kahn and Ostendorf, 2012; Marin and Ostendorf, 2014), unclear sentence boundaries (Kahn et al., 2004), disfluencies (Jamshid Lou and Johnson, 2020; Kahn et al., 2005; Lease and Johnson, 2006), as well as integrating prosodic features into the parsing systems (Tran et al., 2018; Tran and Ostendorf, 2021). On the evaluation side, the closest work to ours is $\text{SPARSE\textsc{EVAL}}$ (Roark et al., 2006), which extends $\text{PARSEVAL}$ to account for speech recognition errors by allowing for word-level insertion, deletion and substitution. In contrast, our metric $\text{STRUCT-IOU}$ applies to the cases where no speech recognizer is applied or available.

Other structured evaluation metrics for parsing. There have been evaluation metrics of abstract meaning representations (AMRs; Cai and Knight, 2013), where two AMR graphs are matched by solving an NP-complete integer linear programming problem. While our work shares the spirit with theirs, we focus on the evaluation of speech constituency parsing over continuous word boundaries. There also exists a polynomial-time exact solution to our optimization problem.

3 Preliminaries

We use real-valued open intervals to represent speech spans for simplicity, although most of the following definitions and conclusions can be easily extended to closed intervals and half-open intervals. Proof of each corollary and proposition can be found in Appendix A.

3.1 Open Inteval Operations

Definition 1. The length of a real-valued open interval $I = (a, b)$, where $a < b$, is $|I| = b - a$.

Definition 2. The intersection size of open inter-
vals $I_1$ and $I_2$ is
$$\mathcal{I}(I_1, I_2) = \begin{cases} 0 & \text{if } I_1 \cap I_2 = \emptyset \\ |I_1 \cap I_2| & \text{otherwise.} \end{cases}$$

**Definition 3.** The **union size** of open intervals $I_1$ and $I_2$ is $\mathcal{U}(I_1, I_2) = |I_1| + |I_2| - \mathcal{I}(I_1, I_2)$.

**Definition 4.** The **intersection over union (IOU)** ratio between open intervals $I_1$ and $I_2$ is
$$\text{IOU}(I_1, I_2) = \frac{\mathcal{I}(I_1, I_2)}{\mathcal{U}(I_1, I_2)}.$$  

Throughout this paper, we will use IOU as the similarity metric between two intervals.

### 3.2 Relaxed Segment Trees

We relax the definition of a segment tree (Bentley, 1977) as follows to represent parse trees.

**Definition 5.** A node $n$ of a relaxed segment tree is a triple $n = \langle I_n, C_n, \ell_n \rangle$, where
1. $I_n = (s_n, e_n)$ is an open interval (i.e., segment) associated with the node $n$, where $s_n < e_n$;
2. $C_n$ is a finite set of disjoint children nodes of $n$: for any $p, q \in C_n (p \neq q)$, $I_p \cap I_q = \emptyset$.
3. $C_n$ is neither an ancestor nor a descendant of $q$ if and only if $n$ is a terminal node;
4. For a nonterminal node $n$, $s_n = \min_{p \in C_n} s_p$, and $e_n = \max_{p \in C_n} e_p$.

**Corollary 5.1.** For nodes $p, n$, if $p \in C_n$, then $I_p \subseteq I_n$.

**Definition 6.** Node $p$ is an **ancestor** of node $q$ if there exists a sequence of nodes $n_0, n_1, \ldots, n_k (k \geq 1)$ such that (i) $n_0 = p$, (ii) $n_k = q$, and (iii.) or any $i \in [k]$, $n_i \in C_{n_{i-1}}$.

**Corollary 6.1.** If node $p$ is an ancestor of node $q$, then $I_p \supseteq I_q$.

**Definition 7.** Node $p$ is a **descendant** of node $q$ if $q$ is an ancestor of $p$.

**Definition 8.** An relaxed segment tree $\mathcal{T} = (\mathcal{r}_\mathcal{T}, \mathcal{N}_\mathcal{T})$ is a tuple, where
1. $\mathcal{r}_\mathcal{T}$ is the root node of $\mathcal{T}$;
2. $\mathcal{N}_\mathcal{T} = \{r_\mathcal{T}\} \cup \{n : n$ is a descendant of $r_\mathcal{T}\}$.

**Example 8.1.** A constituency parse tree over spoken word time ranges (Figure 1a) can be represented by a relaxed segment tree.

**Corollary 8.1.** A relaxed segment tree can be uniquely characterized by its root node.

In the following content, we use $\mathcal{T}(n)$ to denote the relaxed segment tree rooted at $n$.

**Proposition 9.** For a relaxed segment tree $\mathcal{T}$ and $p, q \in \mathcal{N}_\mathcal{T}$, $p$ is neither an ancestor nor a descendant of $q$ unless $p = q$ or $q = r_\mathcal{T}$.

### 4 The STRUCT-IOU Metric

#### 4.1 Problem Formulation

Given relaxed segment trees $\mathcal{T}_1$ and $\mathcal{T}_2$ with node sets $\mathcal{N}_{\mathcal{T}_1} = \{n_{1,i}\}_{i=1}^{\mathcal{N}_{\mathcal{T}_1}}$ and $\mathcal{N}_{\mathcal{T}_2} = \{n_{2,j}\}_{j=1}^{\mathcal{N}_{\mathcal{T}_2}}$, we can align the trees by matching their same-label nodes. Let $n_{1,i} \leftrightarrow n_{2,j}$ denote the matching between the nodes $n_{1,i}$ and $n_{2,j}$.

**Definition 10** (conflicted node matchings; Figure 2). The matchings $n_{1,i} \leftrightarrow n_{2,j}$ and $n_{1,k} \leftrightarrow n_{2,\ell}$ are **conflicted** if any of the following conditions holds:
1. $n_{1,i}$ is an ancestor of $n_{1,k}$, and $n_{2,j}$ is not an ancestor of $n_{2,\ell}$;
2. $n_{1,i}$ is not an ancestor of $n_{1,k}$, and $n_{2,j}$ is an ancestor of $n_{2,\ell}$;
3. $n_{1,i}$ is a descendant of $n_{1,k}$, and $n_{2,j}$ is not a descendant of $n_{2,\ell}$;
4. $n_{1,i}$ is not a descendant of $n_{1,k}$, and $n_{2,j}$ is a descendant of $n_{2,\ell}$.

Intuitively, we would like the alignment to be consistent with the ancestor-descendant relationship between nodes.

The optimal (i.e., maximally IOU-weighted) structured alignment between $\mathcal{T}_1$ and $\mathcal{T}_2$ is given by the solution to the following problem:

**Problem 11** (maximally IOU-weighted alignment),

\[ \text{maximize } \sum_{(n_{1,i} \leftrightarrow n_{2,j})} \text{IOU}(I_{n_{1,i}}, I_{n_{2,j}}), \]

subject to

\[ \sum_{n_{1,i} \leftrightarrow n_{2,j}} \text{IOU}(I_{n_{1,i}}, I_{n_{2,j}}) = 1, \quad n_{1,i} \leftrightarrow n_{1,k} \text{ is conflicted if } n_{1,i} \leftrightarrow n_{2,j} \text{ and } n_{1,k} \leftrightarrow n_{2,\ell}. \]
\[ A^* = \arg \max_A \sum_{i=1}^{\max(|T_1|,|T_2|)} \sum_{j=1}^{\min(|T_1|,|T_2|)} a_{i,j} \text{IOU} \left( I_{n_1,i}, I_{n_2,j} \right) \]

s.t. \[ \sum_j a_{i,j} \leq 1 \forall i \in \min(|T_1|,|T_2|), \] (1)

\[ \sum_i a_{i,j} \leq 1 \forall j \in \min(|T_1|,|T_2|), \] (2)

\[ a_{i,j} + a_{k,l} \leq 1 \]
if \((n_{1,i} \leftrightarrow n_{2,j})\) and \((n_{1,k} \leftrightarrow n_{2,l})\) are conflicted.

\[ A \in \{0,1\}^{\max(|T_1|,|T_2|)} \]
denotes an alignment matrix: \(a_{i,j} = 1\) indicates that the matching \(n_{1,i} \leftrightarrow n_{2,j}\) is selected, otherwise \(a_{i,j} = 0\). The last constraint of Problem 11 ensures that there are no conflicted matchings selected. Equations (1) and (2) imply one-to-one matching between nodes; that is, in a valid tree alignment, each node in \(T_1\) can be matched with at most one node in \(T_2\), and vice versa. The solution to Problem 11 gives the maximal possible sum of IOU over aligned node pairs.

**Definition 12.** The structured average IOU (STRUCT-IOU) between \(T_1\) and \(T_2\) is given by

\[ \text{IOU}(T_1, T_2) = \frac{1}{|T_1| + |T_2|} \sum_{i=1}^{\min(|T_1|,|T_2|)} \sum_{j=1}^{\min(|T_1|,|T_2|)} a_{i,j}^* \text{IOU} \left( I_{n_1,i}, I_{n_2,j} \right), \]

where \(A^* = \{a_{i,j}^*\}\) is the solution to Problem 11.

### 4.2 Solution

We present a polynomial-time algorithm for the exact solution to Problem 11, by breaking it down into structured subproblems and solving them recursively with dynamic programming.

We define the subproblem as follows: given relaxed segment trees \(T_1\) and \(T_2\), we would like to find the maximum IOU weighted alignment of \(T_1\) and \(T_2\), where the roots of \(T_1\) and \(T_2\) are aligned. Without loss of generality, we assume that the root nodes of \(T_1\) and \(T_2\) are both indexed by 1. Formally, Problem 13 (maximum IOU weighted alignment, with root nodes aligned).

**Problem 13**

\[ f_{T_1, T_2} = \max_A \sum_{i=1}^{\min(|T_1|,|T_2|)} \sum_{j=1}^{\min(|T_1|,|T_2|)} a_{i,j} \text{IOU} \left( I_{n_1,i}, I_{n_2,j} \right) \]

s.t. \(a_{1,1} = 1\);
\[ \sum_j a_{i,j} \leq 1 \forall i \in \min(|T_1|,|T_2|), \]
\[ \sum_i a_{i,j} \leq 1 \forall j \in \min(|T_1|,|T_2|), \]
\[ a_{i,j} + a_{k,l} \leq 1 \]
if \((n_{1,i} \leftrightarrow n_{2,j})\) and \((n_{1,k} \leftrightarrow n_{2,l})\) are conflicted.

\[ A \in \{0,1\}^{\max(|T_1|,|T_2|)} \]
is the alignment matrix. While Problems 11 and 13 are not equivalent in principle, Problem 11 can be reduced to Problem 13 within \(O(1)\) time, by adding a dummy root node to each tree that associates with segments covering all the segments in both trees. We now present a polynomial-time solution to Problem 13.

**Definition 14.** Given a node \(n\) of a relaxed segment tree, \(D = (n_1, n_2, \ldots, n_k)\) is an ordered disjoint descendant sequence of \(n\) if

1. (ordered) for any \(i, j \in [k]\) and \(i < j, s_{n_i} < s_{n_j}\), where \(s_{n_i}\) and \(s_{n_j}\) are left endpoint of the associated intervals;
2. (disjoint) for any \(i, j \in [k]\) and \(i \neq j, I_{n_i} \cap I_{n_j} = \emptyset\);
3. (descendant) for any \(i \in [k]\), \(n_i\) is a descendant of \(n\).

**Corollary 14.1.** In an ordered disjoint descendant sequence \(D = (n_1, n_2, \ldots, n_k)\) of \(n\), \(e_{n_i} \leq s_{n_{i+1}}\) for any \(i \in [k-1]\).

The solution to Problem 13 is given by the following recursion:

\[ f_{T_1, T_2} = \text{IOU} \left( I_{r_{T_1}}, I_{r_{T_2}} \right) + \max_{|D_1|} \sum_{i=1}^{|D_1|} f_T(d_{1,i}, T(d_{1,i})); \]

where \(r_{T_1}\) and \(r_{T_2}\) denote the root nodes of \(T_1\) and \(T_2\) respectively; \(|\cdot|\) denotes the length of a sequence; \(D_1 = (d_{1,1}, d_{1,2}, \ldots, d_{1,|D_1|})\) and \(D_2 = (d_{2,1}, d_{2,2}, \ldots, d_{2,|D_2|})\) are same-length ordered disjoint descendant sequences of \(r_{T_1}\) and \(r_{T_2}\) respectively. Equation (3) can be computed within polynomial time, by solving a knapsack-style problem with dynamic programming. Specifically, let

\[ g[T_1, T_2, e_1, e_2] = \max_{|D_1^*| = |D_2^*|} \sum_{i=1}^{|D_1^*|} f_T(d_{1,i}, T(d_{1,i})); \]
We present two example applications of S where the former is our main focus. In each part, the unique features of S and text constituency parsing evaluation (§5.2), solves Problem 13 is \( O(1) \) time, and therefore, the overall time complexity to solve Problem 13 is \( O(n^2m^2) \).

5 Experiments

We present two example applications of STRUCT-IoU: speech constituency parsing evaluation (§5.1) and text constituency parsing evaluation (§5.2), where the former is our main focus. In each part, we show the connection between STRUCT-IoU and existing metrics in appropriate settings and present the unique features of STRUCT-IoU.

5.1 Speech Constituency Parsing Evaluation

5.1.1 Datasets and Setups

We use the NXT-Switchboard (NXT-SWBD; Calhoun et al., 2010) dataset to train and evaluate models, where the parser can access the forced alignment word boundaries in both training and testing stages. We train an off-the-shelf supervised constituency parsing model for speech transcriptions (Jamshid Lou and Johnson, 2020) on the training set of NXT-SWBD, do early-stopping using PARSEVAL F₁ on the development set, and perform all the analysis below on the development set. The model achieves \( F₁ = 85.4 \) and STRUCT-IoU (averaged across sentences)\(^3\) = 0.954 on the standard development set.

5.1.2 Comparison to the PARSEVAL F₁ score

Since the forced alignment word boundaries are accessible by the models, the PARSEVAL \( F₁ \) metric can be directly calculated between the predicted speech constituency parse tree and the ground truth. We compare the values of STRUCT-IoU and PARSEVAL (Sekine and Collins (1997) implementation with default parameters) in the settings with forced-alignment word segmentation (Figure 3), and find a strong correlation between the two metrics.

5.1.3 Analysis: STRUCT-IoU with Perturbed Word Boundaries

In textless speech parsing (Lai et al., 2023; Tseng et al., 2023), the word boundaries are unknown, and the boundaries predicted by the parser are usually

\(^3\)Unless otherwise specified, all STRUCT-IoU scores reported in the paper are computed by averaging across STRUCT-IoU scores of individual sentences. We compare and discuss sentence-level and corpus-level STRUCT-IoU in §5.1.4

---

**Algorithm 1** Polynomial time solution to Equation (3)

**Input:** \( T₁, T₂ \)

\[ g[T₁, T₂, x, y] \leftarrow 0, \forall x, y \]

\[ g[T₁, T₂, x, y] := \max_{x < x', y < y'} g[T₁, T₂, x', y'] \]

\( d₁ \) ← the sequence of all descendants of \( r_{T₁} \), sorted in increasing order of right endpoint

\( d₂ \) ← the sequence of all descendants of \( r_{T₂} \), sorted in increasing order of right endpoint

**Output:** Equation (3) = \( g[T₁, T₂, e_{r_{T₁}}, e_{r_{T₂}}] \)

where \( e₁ \) and \( e₂ \) are arbitrary scalars denoting the constraints of endpoints; \( D₁ = (d₁, \ldots, d₁_{|D₁|}) \) is an ordered disjoint descendant sequence of \( r_{T₁} \), where for any \( j \in [|D₁|] \), the right endpoint of the corresponding node \( ed_{1,j} \leq e₁ \); similarly, \( D₂ = (d₂, \ldots, d₂_{|D₂|}) \) is a disjoint descendant sequence of \( r_{T₂} \) of which the right endpoint of each node does not exceed \( e₂ \). Algorithm 1 computes \( g \) and Equation (3) within polynomial time, and therefore leads to a polynomial-time solution to Problem 13.

**Complexity analysis.** Suppose \( |T₁| = n \) and \( |T₂| = m \). To compute \( f_{T₁, T₂} \), all we need to compute is \( g[T₁, T₂, e_1', e_2'] \) for all \( T₁', T₂', e_1' \) and \( e_2' \). Here, \( T₁' \) and \( T₂' \) enumerate over all subtrees of \( T₁ \) and \( T₂ \), respectively, and \( e_1' \) and \( e_2' \) enumerate over the endpoints of all nodes in both trees, respectively. The update process requires \( O(1) \) time for each \( T₁, T₂, e₁, e₂ \). The edge cases, i.e., \( g \) values of terminal nodes, can be directly computed in \( O(1) \) time, and therefore, the overall time complexity to solve Problem 13 is \( O(n^2m^2) \).
imperfect. As a controlled simulation to such settings, we perturb the forced alignment word boundaries of the predicted parse tree (Figure 4), and calculate the STRUCT-IOU score between the perturbed parse tree and the ground truth over the original forced alignment word boundaries. Specifically, we suppose the word boundaries of a sentence with $n$ words are $B = b_0, b_1, \ldots, b_n,$ and consider the following types of perturbation with a hyperparameter $\delta \in [0, 1]$ controlling the perturbation level:

- **Noise-$\delta$.** We start with $B^{(0)} = B$, and update the boundaries iteratively as follows. For each $i \in [n - 1]$, we randomly draw a number $r_i$ from the uniform distribution $U(-\delta, \delta)$, and let $b_i^{(i)} = b_i^{(i-1)} + r_i \cdot \left( b_{i+\text{sgn}(r_i)}^{(i-1)} - b_i^{(i-1)} \right)$, where $\text{sgn}(\cdot) : \mathbb{R} \rightarrow \{1, -1\}$ denotes the sign function

  \[
  \text{sgn}(x) = \begin{cases} 
  1 & \text{if } x \geq 0; \\
  -1 & \text{if } x < 0. 
  \end{cases}
  \]

  For all $j \neq i$ and $j \in [n]$, we let $b_j^{(i)}$ remain the same as $b_j^{(i-1)}$. Finally, we take $B^{(n-1)}$ as the perturbed word boundaries for the predicted tree.

- **Insert-$\delta$.** We randomly draw a number $r_i$ from the uniform distribution for each boundary index $i \in [n]$. If $r_i < \delta$, we insert a word boundary at the position $b_i^{(i)}$, randomly drawn from the uniform distribution $U(b_{i-1}, b_i)$, breaking the $i^{th}$ spoken word into two (i.e., $[b_{i-1}, b_i^{(i)}]$ and $[b_i^{(i)}, b_i]$).

- **Delete-$\delta$.** Similarly to the insertion-based perturbation, we randomly draw a number $r_i$ from the uniform distribution $U(0, 1)$ for each boundary index $i \in [n - 1]$, and delete the boundary $b_i$ if $r_i < \delta$. Since such boundary deletion may break the predicted tree structure, we use the base model (§5.1.1) to re-predict the parse tree with the new word boundaries, where words concatenated by space are taken as the textual input (Jamshid Lou and Johnson, 2020).

A larger $\delta$ means a higher level of perturbation is applied, and we therefore expect a lower STRUCT-IOU score; $\delta = 0$ means no perturbation is applied, and the STRUCT-IOU score is the same as that for the predicted parse trees with forced alignment word boundaries.

For each $\delta \in \{0.1, 0.2, \ldots, 1.0\}$, starting from the base model (for deletion-based perturbation) or its predicted parse trees (for noise and insertion-based perturbation), we run the perturbation 5 times and report both the mean and the standard deviation of the STRUCT-IOU result after perturbation.

**Results and discussion.** We present how the STRUCT-IOU value changes with respect to $\delta$ for different types of perturbation (Figure 5). The standard deviation is nearly invisible in the figure, showing that our metric is stable under a specific setting. For all three types of perturbation, as desired, a larger $\delta$ leads to a lower STRUCT-IOU score. Among the perturbation types, STRUCT-IOU is the most sensitive to deletion, and the least sensitive to noise-based perturbation. Although the results are not comparable across perturbation.

---

Figure 3: STRUCT-IOU vs. PARSEVAL $F_1$ on NXT-SWBD (Spearman’s correlation $\rho = 0.689$, p-value$=1.79 \times 10^{-54}$). Each dot represents the results of the base model ($F_1=85.4$ on the full development set) on 10 random examples from the development set.

Figure 4: Examples of three types of perturbation: when applicable, the added boundaries are shown in red and the deleted boundaries are shown in blue. Best viewed in color.
types in the most rigorous sense, this reflects the fact that STRUCT-IoU, to some extent, is more sensitive to structural change of the trees than simple word boundary changes.

Although both word boundary insertion and deletion change the predicted tree structures, the former has less impact on the STRUCT-IoU scores. This also aligns with our expectation: boundary insertion only splits some of the spoken words into two and keeps the longer constituents; however, deletion may change significantly the tree structure, especially when it happens at the boundary of two long constituents.

5.1.4 Corpus-Level vs. Sentence-Level Metric

Note that 39.7% utterances in the NXT-SWBD development set contain only one spoken word, and the STRUCT-IoU score of such sentences is always high—the metric degenerates to the IOU score between two intervals. Averaging the STRUCT-IoU scores across all sentence pairs in the dataset may therefore overly emphasize these short utterances. To address this, we introduce the corpus-level STRUCT-IoU score as an alternative, where Definition 12 is modified as follows:

**Definition 15.** The corpus-level STRUCT-IoU between two sets of parsed trees \( D_1 = \{ T_{1,k} \} \) and \( D_2 = \{ T_{2,k} \} \) is given by

\[
\text{IOU}(D_1, D_2) = \frac{\sum_{k=1}^{\mid D_1 \mid} (\mid T_{1,k} \mid + \mid T_{2,k} \mid) \text{IOU}(T_{1,k}, T_{2,k})}{\sum_{k'=1}^{\mid D_2 \mid} \mid T_{1,k'} \mid + \mid T_{2,k'} \mid},
\]

where \( \mid D_1 \mid = \mid D_2 \mid \), and a pair of \( T_{1,k} \) and \( T_{2,k} \) denotes the parse trees of the \( k^{th} \) sentence in the corpus respectively.

We compare the corpus-level and sentence-level STRUCT-IoU scores (Figure 6). As desired, the corpus-level STRUCT-IoU score has lower absolute values than the sentence-level one, and the difference is more significant when longer sentences are considered. A similar phenomenon has been found in text constituency parsing (Kim et al., 2019) as well, where corpus-level PARSEVAL \( F_1 \) scores are lower than sentence-level ones.

5.2 Evaluation of Text Constituency Parsing

We extend our experiment to the evaluation of text constituency parsing. In this part, we suppose every written word corresponds to a segment of the same length—analogously, this can be considered as speech parsing with evenly distributed word boundaries, for both predicted and ground-truth trees.

5.2.1 Correlation with PARSEVAL \( F_1 \) Scores on the Penn Treebank

We use the Penn Treebank (PTB; Marcus et al., 1993) dataset to train and evaluate Benepar (Kim et al., 2018), a state-of-the-art text constituency parsing model, doing early-stopping using labeled PARSEVAL \( F_1 \) on the development set. The base model achieves PARSEVAL \( F_1 = 94.4 \) and STRUCT-IoU (averaged across sentences) = 0.962 on the standard development set.

We compare the STRUCT-IoU scores with the PARSEVAL \( F_1 \) scores on the development set (Figure 7). As in the speech parsing experiment, we find a strong correlation between the two metrics, showing that STRUCT-IoU is consistent with the
existing metric in the text parsing domain.

5.2.2 STRUCT-IoU vs. PARSEVAL \( F_1 \) on Syntactically Ambiguous Sentences

We consider a special setting of parsing syntactically ambiguous sentences, where the syntactically plausible parse tree of a sentence may not be unique (see examples in Figure 8). We simplify the case shown in Figure 8 and generate synthetic sentences with syntactic ambiguity with the template \( N \{ P N \}^n \), where \( P \) denotes a preposition and \( N \) denotes a noun, and \( n \) determines how many times the \( P N \) pattern is repeated. For \( N \{ P N \}^2 \), the two potential parse trees are shown in Figure 9.

We compare the PARSEVAL and STRUCT-IoU in the following scenarios, choosing a random syntactically plausible parse tree as the ground truth:

- **Ground truth vs. random parse trees**, where the random parse trees are constructed by recursively combining random consecutive words (or word groups) into a binary tree. We construct 100 random parse trees and report the average.
- **Ground truth vs. syntactically plausible parse trees**, where we report the lowest possible score between the ground truth and other syntactically plausible trees.

As shown in Table 1, the lowest possible PARSEVAL \( F_1 \) score between the ground truth and another syntactically plausible tree is significantly lower than the score achieved by meaningless random trees; however, STRUCT-IoU consistently assigns higher scores to the syntactically plausible parses, showing more tolerance to syntactic ambiguity.

6 Conclusion and Discussion

In this paper, we present STRUCT-IoU, the first metric that computes the similarity between two parse trees over continuous spoken word boundaries. STRUCT-IoU enables the evaluation of textless speech parsing (Lai et al., 2023; Tseng et al., 2023), where no text or speech recognizer is used or available to parse spoken utterances.

In the canonical settings of text and speech parsing, STRUCT-IoU serves as a complement to the existing evaluation metrics (Black et al., 1991; Roark et al., 2006). In particular, STRUCT-IoU shows a higher tolerance to potential syntactic ambiguity under certain scenarios, providing an alternative interpretation of the parsing quality.
7 Limitations

STRUCT-IoU is designed to evaluate constituency parse trees over continuous spoken word boundaries, and is not directly applicable to evaluate other types of parses, such as dependency parse trees; however, it may be extended to evaluate other types of parse trees by modifying the alignment constraints. We leave the extension of STRUCT-IoU to other types of parses as future work. We do not foresee any risk of STRUCT-IoU being used in harmful ways.

References


Sasha Calhoun, Jean Carletta, Jason M Brenier, Neil Mayo, Dan Jurafsky, Mark Steedman, and David Beaver. 2010. The nxt-format switchboard corpus: a rich resource for investigating the syntax, semantics, pragmatics and prosody of dialogue. Language resources and evaluation, 44:387–419.


Appendix

A Proof of Corollaries and Propositions

We present the proof of the corollaries mentioned in the main content as follows.

**Corollary 5.1** For nodes \( p, n \), if \( p \in C_n \), then \( I_p \subseteq I_n \).

*Proof.* According to the definition of open intervals and Definition 5 (3),

\[
a_n \leq a_p < b_p \leq b_n
\]

\[
\implies I_p = (a_p, b_p) \subseteq (a_n, b_n) = I_n.
\]

**Corollary 6.1** If node \( p \) is an ancestor of node \( q \), then \( I_p \supseteq I_q \).

*Proof.* According to Definition 6, there exists a sequence of nodes \( n_0, n_1, \ldots, n_k (k \geq 1) \) such that (1) \( n_0 = p \), (2) \( n_k = q \) and (3) for any \( i \in [k] \), \( n_i \in C_{n_{i-1}} \).

Corollary 5.1 implies that for any \( i \in [k] \), \( I_{n_{i-1}} \supseteq I_{n_i} \implies I_{n_0} \supseteq I_{n_k} \implies I_p \supseteq I_q \).

**Corollary 8.1** A relaxed segment tree can be uniquely characterized by its root node.

*Proof.* (\( \Rightarrow \)) Definition 8 implies that each relaxed segment tree has one root node.

(\( \Leftarrow \)) Given a specific node \( n \), we have the unique set \( \mathcal{N} = \{n\} \cup \{n' : n' \text{ is a descendant of } n\} \), and therefore extract the set of all nodes in the relaxed segment tree rooted at \( n \).

**Proposition 9** For a relaxed segment tree \( T \) and \( p, q \in N_T \), \( p \) is neither an ancestor nor a descendant of \( q \) \( \iff I_p \cap I_q = \emptyset \).

*Proof.* (\( \Rightarrow \)) Let \( z \) denote the least common ancestor of \( p \) and \( q \). There exists \( p', q' \in C_z (p' \neq q') \) such that \( I_{p'} \supseteq I_p \) and \( I_{q'} \supseteq I_q \); therefore

\[
I_p \cap I_q \subseteq I_{p'} \cap I_{q'} \overset{\text{Definition 5 (2)}}{=} \emptyset \implies I_p \cap I_q = \emptyset.
\]

(\( \Leftarrow \)) If \( I_p \cap I_q = \emptyset \), according to Definition 5 (3) and Definition 6, \( p \) is not an ancestor of \( q \) and vice versa.

**Corollary 14.1** Given an ordered disjoint descendant sequence \( S = (n_1, n_2, \ldots, n_k) \) of \( n \), for any \( i \in [k - 1] \), \( b_{n_i} \leq a_{n_{i+1}} \).

*Proof.* If there exists \( i \in [k - 1] \) such that \( b_{n_i} > a_{n_{i+1}} \), then

\[
I_{n_i} \cap I_{n_{i+1}} = (a_{n_i}, b_{n_i}) \cap (a_{n_{i+1}}, b_{n_{i+1}}) = \{x : \max(a_{n_i}, a_{n_{i+1}}) < x < \min(b_{n_i}, b_{n_{i+1}})\} = \{x : a_{n_{i+1}} < x < \min(b_{n_i}, b_{n_{i+1}})\}
\]

*(Definition 14 (1)).*

Since \( b_{n_{i+1}} > a_{n_{i+1}} \) (definition of open intervals),

\[
\exists a_{n_{i+1}} < \min(b_{n_i}, b_{n_{i+1}}) \implies I_{n_i} \cap I_{n_{i+1}} \neq \emptyset.
\]

This conflicts with Definition 14 (2).

B Checklist Details

We discuss the additional checklist details in the following content.

**B2: Licenses of Scientific Artifacts.** *EVALB* (Sekine and Collins, 1997), an open-source implementation of *PARSEVAL* (Black et al., 1991), is free and unencumbered software released into the public domain. *PARSEVAL* (Roark et al., 2006) is licensed under the Apache License, Version 2.0.